Sequence correlations shape protein promiscuity

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We predict analytically that diagonal correlations of amino acid positions within protein sequences statistically enhance protein propensity for nonspecific binding. We use the term “promiscuity” to describe such nonspecific binding. Diagonal correlations represent statistically significant repeats of sequence patterns where amino acids of the same type are clustered together. The predicted effect is qualitatively robust with respect to the form of the microscopic interaction potentials and the average amino acid composition. Our analytical results provide an explanation for the enhanced diagonal correlations observed in hubs of eukaryotic organismal proteomes [J. Mol. Biol. 409, 439 (2011)]. We suggest experiments that will allow direct testing of the predicted effect. © 2011 American Institute of Physics. [doi:10.1063/1.3624332]

I. INTRODUCTION

Recent experimental evidences that proteins within a cell maintain a high degree of nonspecificity have challenged the understanding of molecular mechanisms providing the specificity of protein-protein binding.1–3 Such nonspecific binding is often termed protein “promiscuity.” Numerous organismal-scale measurements of binary protein-protein interactions (PPI) suggest that organismal proteomes possess a higher degree of nonspecific binding.4–10 The dominant amount of such experimental PPI data comes from the high-throughput yeast two-hybrid (Y2H)7,11,12 and affinity purification followed by mass spectrometry (AP/MS).13–15 Although these experiments do not provide dynamical and functional properties of interactions,7 they do provide a snapshot of binary, physical interactions that might be functionally important in a living cell. These experiments show that a small fraction of proteins (termed “hubs”) are physically interacting with tens and even hundreds of partners. It appears that protein promiscuity is a selectable trait enabling proteins to adopt more efficiently to changing conditions or emerging needs within a living cell.1

The key question is what makes a protein promiscuous, i.e., prone to nonspecific interactions? Are there generic sequence signatures of promiscuity? In this paper we predict one such generic signature. We show analytically that protein sequences with enhanced correlations of sequence positions of amino acids of the same type generally represent more promiscuous sequences. We use the term “diagonal” to describe such correlations. Intuitively, sequence “correlations” mean statistically significant repeats of sequence patterns. Our findings suggest that symmetry properties and strength of sequence correlations are important factors that control global connectivity properties of PPI networks.

Using a bioinformatics analysis, we have recently shown that hubs of eukaryotic (e.g., yeast and human) proteomes possess a higher level of diagonal correlations compared to non-hubs.16 In particular, we have shown that in human PPI network, His, Phe, Ile, Pro, Gly, and Tyr exhibit significantly stronger diagonal correlations in hubs than in non-hubs.16 Here, we develop an analytical theory that explains why this might be the case. Since many hub proteins detected in Y2H and AP/MS experiments are confirmed to be functionally multi-specific in vivo, our theoretical predictions suggest that enhanced nonspecific binding and functional multi-specificity might be tightly linked. We suggest that a significant fraction of functionally multi-specific proteins might be inherently highly promiscuous.

This article is organized as follows. First, we introduce a precise, statistical measure of promiscuity. Second, we present a simple model that describes protein-protein binding. This model uses a two-letter alphabet, linear protein sequences, and it is analytically solvable in the Gaussian approximation. We develop a stochastic procedure allowing us to design protein sequences with a controlled symmetry and strength of sequence correlations. We analyze statistical, interaction properties of such sequences. Third, we qualitatively describe possible implications of our results for protein folding. We conclude by proposing experiments that will allow direct testing of the predicted effect.

II. RESULTS AND DISCUSSION

A. Statistical measure for interaction promiscuity

We begin by introducing a statistical measure of promiscuity for a given protein, A. Such measure can be defined as the probability distribution of the interaction energies, $P(E_A)$, of this protein with a set of target proteins, where $E_A$ is the interaction energy between protein A and a protein from the target set. Now we can compare the promiscuity of two proteins A and B interacting with the same target set, assuming that the corresponding average interaction energies are the same, $\langle E_A \rangle = \langle E_B \rangle$. This latter target set is not supposed to be
optimized in any way for stronger binding with either protein A or protein B. If the dispersion, $\sigma_A$, of $P(E_A)$ is greater than the dispersion, $\sigma_B$, of $P(E_B)$, then protein A is statistically more promiscuous than protein B. This is because if $\sigma_A > \sigma_B$, the mean free energies of binding obey the inequality, $F_A < F_B$. In particular, we have recently shown analytically that if $P(E_A)$ and $P(E_B)$ are Gaussian, then the mean free energy difference always satisfies, $F_A - F_B = -(\sigma^2_A - \sigma^2_B)/2k_B T$. The assumption that $\langle E_A \rangle = \langle E_B \rangle$ corresponds to the constraint that the sequences of two proteins A and B have the same average amino acid composition (see below). The latter constraint is necessary for a fair comparison of promiscuities, since the differences in the average amino acid composition would produce a trivial shift of the average interaction energies. The predicted effect is induced exclusively by sequence correlations and goes beyond the mean-field. The above argument holds true if instead of two proteins A and B, we consider two sets of proteins $\{A_1, \ldots, A_M\}$ and $\{B_1, \ldots, B_M\}$ interacting with the same set of random binders, as above, and characterized by analogous distributions of the binding energies, $P(E_A)$ and $P(E_B)$. Our objective is to compute the properties of $P(E)$ for model proteins with controllable strength and symmetry of sequence correlations, interacting with a set of random binders, reflecting the statistics of interaction strengths in crowded cellular environments.

B. Analytical model for “random” and “designed” interacting sequences

We introduce now a simple model for “random” and “designed” (or “correlated”) protein-like, linear sequences, Fig. 1. Despite its one-dimensional origin, the model is not exactly solvable because of the generally long-range nature of the potentials that we use below. For simplicity we use a minimalistic sequence alphabet with only two types of amino acids. Random sequence is obtained by distributing $N_p$ and $N_h$ amino acids of types P and H, respectively, at random within a linear sequence of the total length $L = N_p + N_h$. Our simplistic approach therefore does not take into account the folding of the sequence. The average linear fraction of P and H amino acids is thus fixed and given by $\phi_p = N_p/L$ and $\phi_h = N_h/L$, respectively. The notion of P and H types stands here just in order to distinguish between two different amino acid types, and it does not constrain our conclusions to just hydrophobic and polar types. Our conclusions hold qualitatively true for any number of amino acid types.

After each random sequence is generated, amino acid identities are fixed and not allowed to change their positions. A correlated sequence is obtained using the following stochastic procedure. First, we generate a random sequence as described above. Second, we allow amino acids to anneal at a given “design” temperature, $T_d$. We note that our notion of the “designed” sequences stands to describe the existence of positional correlations of amino acids within linear sequences and not the folding. We thus impose that amino acids within the sequence under the design procedure interact through the pairwise additive design potential, $U_{\alpha\beta}(x)$. The intra-sequence interaction energy for any given amino acid realization:

$$E_{\text{intra}} = \frac{1}{2} \int \phi_p(x)U_{pp}(x - x')\phi_p(x')dx dx' + \frac{1}{2} \int \phi_h(x)U_{hh}(x - x')\phi_h(x')dx dx' + \int \phi_h(x)U_{hp}(x - x')\phi_p(x')dx dx', \quad (1)$$

where $\phi_p(x)$ and $\phi_h(x)$ are the local, linear fraction densities of P and H amino acids, respectively. The average composition of P and H amino acids is fixed by the values, $\phi_{p,0}$ and $\phi_{h,0}$, respectively, and we impose that the total fraction of amino acids at each sequence position, $x$, is unity, $\phi_p(x) + \phi_h(x) = 1$. Here $U_{pp}(x)$, $U_{hh}(x)$, and $U_{hp}(x)$ is the interaction potential between PP, HH, and HP amino acid pairs, respectively. We also note that $\phi_p(x)$ can be represented in the form: $\phi_p(x) = \phi_{p,0} + \delta\phi_p(x)$, where $\delta\phi_p(x)$ is the deviation of the local density of P-type amino acids from its average value, and analogously, $\phi_h = \phi_{h,0} + \delta\phi_h(x)$. The only two assumptions about the interaction potentials, $U_{\alpha\beta}(x)$, used in the sequence design procedure are that they are pairwise additive and have a finite range of action. We emphasize that in Eq. (1) only a single combination of the potentials is relevant, $U(x) = U_{pp}(x) + U_{hh}(x) - 2U_{hp}(x)$ (see below).

We note that below, we also use the Monte-Carlo (MC) stochastic design procedure that performs actual amino acid swaps with the Metropolis criterion for the energy change. Our next step is to analyze the probability distribution $P(E)$ of the interaction energy, $E$, between random and
correlated sequences. Every pair of interacting sequences thus consists of one random and one correlated sequence superimposed in a parallel configuration, thus the problem is a quasi one-dimensional one. We show below that enhanced correlations between amino acids of the same type lead to the broadening of the distribution, $P(E)$. The resulting binding free energy computed from the broader distribution will be lower than the binding free energy computed from a narrower different values of the design temperature, $\nu_p$ b. broadening of the distribution, posed in a parallel configuration, thus the problem is a quasi correlated sequences. Every pair of interacting sequences thus and therefore all the different distributions $V_{hp}$ the same for random and correlated sequences. We emphasize $U_{hp}$ its average value, and analogously for $U_{hp}(\rho) = \phi_{h0} + \delta \nu_{hp}(\rho)$. We thus assume that the average amino acid composition is the same for random and correlated sequences. We emphasize that the inter-sequence interaction potentials, $V_{pp}(\rho), V_{hb}(\rho)$, and $V_{hp}(\rho) = V_{ph}(\rho)$, need not be identical to the potentials $U_{pp}(x), U_{bh}(x)$, and $U_{hp}(x)$ used in the sequence design procedure to generate sequences with a controlled symmetry and strength of correlations. We note that in Eq. (2), analogously to Eq. (1), only a single combination of the potentials is relevant, $V(x) = V_{pp}(x) + V_{hb}(x) - 2V_{ph}(x)$ (see below). We now describe in details the effect of the potentials $V_{ap}(x)$ and $U_{ap}(x)$ on the properties of $P(E)$.

The probability distribution for the interaction energies between the random and correlated sequences, $P(E)$, is characterized by its mean, $\langle E \rangle$, and by the variance, $\sigma^2$. In particular, in order to compute $P(E)$, we generate the ensemble of interacting sequence pairs, where each pair consists of a random sequence and “designed” (i.e., correlated) sequence. The interaction energy between the interacting sequence pairs, where each pair consists of a random sequence and “designed” (i.e., correlated) sequence. The interaction energy is performed in order to diagonalize the quadratic forms, and obtain the general case of non-Gaussian distribution, in the general case, and thus the larger is $\hat{V}(k)$, the larger is $U(k)$, when the Gaussian fluctuation model breaks down. In addition, the Fourier transform that we implemented in order to diagonalize the quadratic forms, and obtain Eq. (6), is strictly justified in the continuous limit only, for the infinitely long sequence. The lower and upper physical bounds for the wave-vector, $k$, are $k \sim 1/L$ and $k \sim 1/a_0$, respectively, where $L$ is the sequence length, and $a_0$ is the length-scale of the order of amino acid size. We emphasize that the probability distribution, $P(E)$, is not the Gaussian distribution, in the general case, and thus the analysis of higher-order moments might be required to characterize $P(E)$ at sufficiently low magnitudes of the design temperature, when the correlation length of sequence correlations gets sufficiently large. The analysis of exactly solvable, Ising-type model for protein-DNA interactions suggests that in the general case of non-Gaussian distribution, $P(E)$, all the key conclusions hold qualitatively true.20

The analysis of Eq. (6) leads to the two key conclusions. First, the more negative is the “design” potential, $U(x)$, the larger is $\sigma$. Taking into account the definition of $U = U_{pp} + U_{bh} - 2U_{ph}$, one concludes that in order to increase $\sigma$ one needs to design the sequences with the enhanced correlations in the positions between the residues of similar types. This means that correlated sequences where amino acids of the same type are clustered together will be the more

\[ P_d[\delta \phi_p(x)] = C_1 \exp \left[ -\int \frac{\delta \phi_p^2(x)}{2\phi_{p0}\phi_{h0}} dx \right] \exp(-E_{\text{intra}}/k_BT_d). \]
promiscuous ones. Second, such correlated sequences will interact statistically stronger (than non-correlated sequences would do) with any arbitrary sequences independently on the sign of the inter-residue interaction potential, \( V = V_{pp} + V_{hh} - 2V_{ph} \). Third, if the design potential is overall positive, \( U > 0 \), designed sequences will be even less promiscuous than random sequences. We emphasize that the predicted effects are generic and qualitatively independent on the specific form and even sign of the microscopic interaction potentials, \( V_{ap} \), and on the average amino acid composition of the sequences.

We note that the predicted effect gets even stronger when both interacting sequences are “designed” (i.e., correlated). In the latter case the variance, \( \sigma_{d,d} \), of the corresponding \( P(E) \) is a straightforward generalization of Eq. (6):

\[
\sigma_{d,d}^2 = 4L \int \frac{dk}{2\pi} |\tilde{V}(k)|^2 \times \frac{1}{(1/\phi_{p,0}\phi_{h,0} + \tilde{U}_1(k)/k_BT_{d1})(1/\phi_{p,0}\phi_{h,0} + \tilde{U}_2(k)/k_BT_{d2})},
\]

where \( U_1(x) \) and \( U_2(x) \) are defined analogously to \( U(x) \) for each of the interacting sequences; and \( T_{d1} \) and \( T_{d2} \) are the design temperatures for the first and second sequence, respectively. If both “design” potentials, \( U_1(x) \) and \( U_2(x) \), are overall negative, then \( \sigma_{d,d} > \sigma \), and thus in the latter case the sequences will be statistically more promiscuous than in the case when only one of the interacting sequences is “designed” (Eq. (6)). We stress that the interacting sequences are designed independently and not optimized in any way towards stronger binding. Therefore, the observed effect of statistically enhanced binding corresponds to nonspecific (promiscuous) binding. We note that in both cases, Eqs. (6) and (7), the greatest \( \sigma \) and \( \sigma_{d,d} \) are achieved when the average amino acid composition of sequences is uniform, \( \phi_{p,0} = \phi_{h,0} = 1/2 \).

In order to verify our theoretical predictions, we first perform the standard MC annealing procedure to design correlated sequences. We begin with generating a random sequence starting with a given amino acid composition. We next perform the MC stochastic design procedure, where amino acids within the sequence are allowed to exchange their positions, and each sequence configuration has the Boltzmann weight, \( \sim \exp(-E_{\text{int}}/k_BT_d) \), where \( E_{\text{int}} \) is the internal energy of the sequence in a given configuration by Eq. (1). The MC design procedure is stopped after a certain number of MC moves, and the resulting annealed configuration is accepted as the final, designed configuration for a given sequence. The lower \( T_d \) is, the stronger are the correlations within the sequences. Intuitively, stronger correlations correspond to repetitive sequence patterns with a longer correlation length. The properties of the correlated patterns depend critically on the sign of the interaction potentials \( U_{ap}(x) \) used in the design procedure. If the effective design potential \( U = U_{pp} + U_{hh} - 2U_{hp} \) is overall negative (this corresponds to the attraction between the amino acids of similar types), the correlated patterns will have the form of repetitive residues of the same type, for example: HHHHPPPP... If however, the potential \( U = U_{pp} + U_{hh} - 2U_{hp} \) is overall positive, the correlated patterns will have the form of the alternating H and P residues, for example: HHPHPHPHPHPHP... To characterize the correlation properties of the sequences quantitatively, we introduce the normalized correlation function:

\[
n_{ap}(x) = g_{ap}(x)/\langle g_{ap}(x) \rangle_r,
\]

where \( g_{ap}(x) \) is proportional to the probability to find a residue of the type \( \alpha \) separated by the distance \( x \) from a residue of the type \( \beta \), and \( g_{ap}(x) \) is the corresponding probability for the randomized sequence, and \( \langle g_{ap}(x) \rangle_r \) corresponds to the averaging with respect to different realizations of randomized sequences. The computed correlation functions are represented in Fig. 2 at the value of \( k_BT_d = 1 \) (in the units of \( k_BT \)). For the entirely uncorrelated (random) sequences, all the matrix elements of \( n_{ap}(x) \) are equal to unity, Fig. 2. The clustering of amino acids of similar types corresponds to \( n_{av}(x) > 1 \), Fig. 2.

The next step is to compute numerically the properties of the probability distribution, \( P(E) \), of the interaction energies, \( E \), between random and designed sequences (i.e., each interacting pair consists of a random and designed sequences). The results of these calculations are shown in Fig. 3. We computed \( P(E) \) at different values of \( T_d \) and we represented the results as a ratio between the dispersion of \( P(E) \), \( \sigma = \sigma_{d,r} \), and the dispersion of the corresponding probability distribution where both sequences are entirely random, \( \sigma_{r,r} \), and the latter corresponds to the case of a vanishing design potential, \( U_{ap} = 0 \). We used here the inter-residue interaction potential, \( V_{pp} = V_{hh} = -1 \), and \( V_{hp} = 1 \) (in the units of \( k_BT \)), and we assumed that the nearest neighbor and the next-nearest neighbor amino acids can interact between the two sequences. The analytical result computed from Eq. (6) is also plotted in Fig. 3. As expected, the Gaussian fluctuation model becomes accurate at small values of the ratio, \( U(a)/k_BT_d \ll 1 \), where \( a \) is the potential range. The inset
of Fig. 3 shows the computed $P(E)$ in the case of designed-random and random-random sequence pairs, respectively. The key conclusion here is that in accordance with the analytical predictions, the dispersion of the interaction energies of the designed-random, $\sigma = \sigma_{d,r}$, and random-random, $\sigma = \sigma_{r,r}$, sequence pairs at different values of the design temperature, $T_d$ (circles). The error bars are smaller than the symbol size. The uniform amino acid composition was adopted: 50% P and 50% H residues in each sequence. Thin curve represents the corresponding analytical result, Eq. (6). Inset (adopted from Ref. 16): Computed probability distribution function, $P(E)$, for the interaction energies between the pairs of two random sequences (black), and pairs consisting each of a random and a designed sequences, where the designed sequences were generated at $T_d = 1$ (in the units of $k_B T$) (red). The energy $E$ is normalized per one amino acid.

FIG. 3. Computed ratio between the dispersions of the $P(E)$ for the interaction energies of the designed-random, $\sigma = \sigma_{d,r}$, and random-random, $\sigma = \sigma_{r,r}$, sequence pairs at different values of the design temperature, $T_d$ (circles). The error bars are smaller than the symbol size. The uniform amino acid composition was adopted: 50% P and 50% H residues in each sequence. Thin curve represents the corresponding analytical result, Eq. (6). Inset (adopted from Ref. 16): Computed probability distribution function, $P(E)$, for the interaction energies between the pairs of two random sequences (black), and pairs consisting each of a random and a designed sequences, where the designed sequences were generated at $T_d = 1$ (in the units of $k_B T$) (red). The energy $E$ is normalized per one amino acid.

Our simplified analysis suggests that such enhanced diagonal correlations generically widen the energy spectrum of nonspecific states within the proteins, which leads to the lowering of the energy for disordered conformations. We use the term “intra-protein promiscuity” to describe increased probability for thermodynamically allowed, non-native conformational states. Specifically, it was shown that statistics of energies of misfolded conformations which are structurally dissimilar to native state obeys the random energy model, so that the energy gap between the native state and the lowest energy misfolded conformation can be estimated as:

$$\Delta = E_{\text{nat}} - \langle E \rangle - \frac{\sigma}{\sqrt{2 \ln \gamma}},$$

where $E_{\text{nat}}$ is effective free energy of native state (which incorporates energetic and entropic solvent effects, as well as the entropy of small motions around the native conformation), $\sigma$ is the standard deviation of the energies of misfolded conformations, and $\gamma$ is effective number of conformations per amino acid. The physical intuition behind Eq. (9) is that the total energy of a protein in any conformation is a sum of energies of many interacting fragments leading to the Gaussian distribution of energies of protein conformations. To that end, the one-dimensional model developed in this paper applies to the interaction of fragments, providing a corrected value of $\sigma$. In particular, diagonal correlations increase the variance of energies of misfolded conformations, decreasing the energy gap, $\Delta$, which leads to a higher likelihood that the protein chain will end up in a misfolded conformation and a slower folding rate to the native state. While these considerations are suggestive, a straightforward analysis based on the replica theory of protein-like heteropolymers is required to quantitatively assess the impact of diagonal correlations on stability of unique folded states of proteins. Such analysis is forthcoming.

C. Implications of sequence correlations for protein folding

A key limitation of our theoretical analysis is the fact that the presented simplified model does not explicitly take into account protein folding, and therefore, underestimates the effect of longer-range sequence correlations induced by the presence of a protein chain. Taking protein folding into account should provide additional insights into the effect of long-range sequence correlations on protein promiscuity and structural disorder. Elucidation of the latter issue is the subject of our future work.

Using a bioinformatics analysis, we have recently shown that enhanced diagonal sequence correlations are strongly overrepresented in structurally disordered proteins, as compared to structurally ordered proteins (such as all-alpha and all-beta proteins). In particular, we have observed that in a set of experimentally known disordered proteins, diagonal correlations are significantly enhanced for Gly, Tyr, Arg, Trp, Ser, Glu, Pro, Asp, Gln, Ala, Lys, and Thr. Using a bioinformatics analysis, we have recently shown that enhanced diagonal sequence correlations are strongly overrepresented in structurally disordered proteins, as compared to structurally ordered proteins (such as all-alpha and all-beta proteins). In particular, we have observed that in a set of experimentally known disordered proteins, diagonal correlations are significantly enhanced for Gly, Tyr, Arg, Trp, Ser, Glu, Pro, Asp, Gln, Ala, Lys, and Thr. In general, the longer is the length scale of homo-oligomer repeats, the wider the inter-protein interaction energy spectrum, and the more promiscuous are the sequences. This effect is qualitatively robust with respect to the specific form and even sign of the microscopic inter-sequence interaction potential, and it is controlled by the length scale and symmetry of sequence correlations. Despite the one-dimensional nature of our model, its results are directly applicable to protein-protein interactions.
interaction networks since the most recent, whole-organism experimental and bioinformatics data suggest that 15%-40% of all protein-protein interactions are mediated by linear sequence motifs, and not by large protein surfaces.30 Our analytical predictions provide an explanation for the enhanced diagonal correlations observed in hubs of human and yeast PPI networks.16 Our key objective for the future theoretical analysis is to take into account the effect of protein folding on inter-protein interaction properties.

The widening of the interaction energy spectrum, $P(E)$, in the presence of enhanced diagonal correlations, which is the key prediction of this paper, can be understood intuitively in the following way. Due to enhanced clustering of amino acids of the same type, Fig. 1(c), a protein sequence interacting with a set of random binders will locally, along its length, encounter either a more significant amount of favorable contacts, or on the contrary, a more significant amount of unfavorable contacts, compared with the sequence lacking such correlations, Fig. 1(a). The latter property stems from the fact that each amino acid in one sequence can interact with more than one, nearest-neighbor amino acid in the other sequence, and hence, the clustering of amino acids of the same type induces an enhanced cooperativity, which in turn, enhances the fluctuations of $E$.

We also note that qualitatively, not only enhanced clustering of entirely identical amino acids (we used the term “diagonal correlations” to describe such clustering) should lead to enhanced protein promiscuity. We suggest that sequences with enhanced clustering of amino acids possessing similar structural and physicochemical properties, for example, Asn and Glu, should also exhibit the predicted effect.

There are several possible strategies to test our predictions. The direct experimental test would utilize a protein chip technology. The target protein data set would be attached to the chip surface. The test proteins or peptides would be synthesized with a varying strength and symmetry of sequence correlations but keeping the average amino acid composition fixed. Titration experiments should allow measuring directly the binding affinity as a function of sequence correlation properties. We expect that protein sequences with enhanced diagonal correlations will generically represent more promiscuous sequences. Another possibility is to use a recent genome-wide protein over-expression analysis.33 Since the over-expression of highly promiscuous proteins should presumably be toxic to a cell, the correlation analysis of such toxic proteins (hundreds of them are known) will show whether the predicted effect plays a significant role in a living cell.34

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