

The Accelerating Universe: A Challenge to Fundamental Physics

Ram Brustein



אוניברסיטת בן-גוריון

Irit maor
(BGU → Cambridge)
P. Steinhardt (Princeton)

PRL 86 (2001),
PRD 65 (2002),
PRD 67 (2003)



- ✧ Evidence for accelerated expansion
- ✧ Interpretation – “phenomenology”
- ✧ Explanation – “theory”

Et pourtant il accélère !

La concordance de toutes ces expériences a fait sursauter plus d'un cosmologiste. À l'aube du XXI^e siècle, il devient clair que 95 % de l'Univers nous est totalement étranger ! Les astrophysiciens s'aperçoivent que toutes leurs théories ne se fondent que sur l'observation des cinq petits pour cent visibles de l'énergie totale [fig. 4]. De quoi rendre sceptique le commun des mortels, mais pas les scientifiques, qui continuent à bâtir leur édifice théorique contre vents et marées. Leur plus grand défi est aujourd'hui de dévoiler la nature de cette énergie noire,

מפץ גדול חם: המודל הסטנדרטי

Geometry

$$ds^2 = -dt^2 + a(t)^2 dr^2$$



GR:

$$a(t), 1+z = a(now)/a(t), H = \dot{a}/a$$

Matter

$$\rho(z), p(z), w(z) = p/\rho.$$

$$3H^2 = 8\pi G_N \rho$$

$$\dot{H} = -4\pi G_N (\rho + p)$$

$$\dot{\rho} + 3H(\rho + p) = 0$$

ρ_C - critical density
(Euclidean space)

$$\Omega_X = \rho_X / \rho_C$$

Accelerated expansion ?!

$$3H^2 = 8\pi G_N \rho$$

$$\dot{H} = -4\pi G_N (\rho + p)$$

$$\dot{\rho} + 3H(\rho + p) = 0$$

$$\ddot{a}/a = \dot{H} + H^2$$

$$\ddot{a} > 0 \Rightarrow \rho + 3p < 0$$

$$w < -1/3$$

Radiation

$$\rho = 3p, w = 1/3$$

Matter

(normal and dark)

$$p=0, w = 0$$

Attractive gravity +

“normal” matter →

decelerated expansion

Mapping the Universe

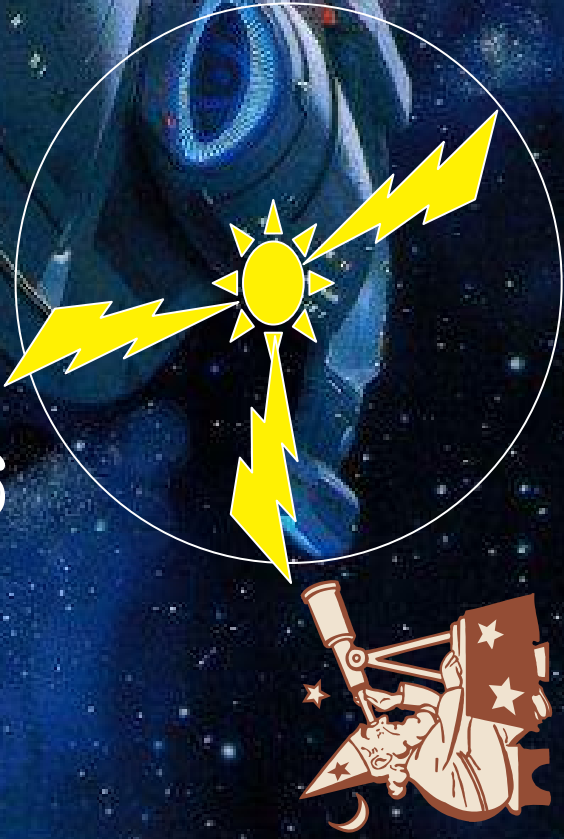
ratio of luminosity \mathcal{L} to flux \mathcal{F}

$$d_L = \sqrt{\frac{\mathcal{L}}{4\pi\mathcal{F}}} = (1+z)r$$



Luminosity – energy/time emitted by source

Flux – energy /time/area absorbed by detector



Due to expansion:

Energy/time $\nabla (1+z)^2$

(1+z) red shift of energy

Need

“standard candles”

Luminosity distance d_L vs. redshift z : Hubble Diagram

For light

$$-dt^2 + a^2 dr^2 = 0$$

$$H = -\frac{1}{a} \frac{da}{dt}$$



$$dz = -\frac{da}{a^2}$$

$$r = \int_1^{1+z} \frac{dx}{H}$$

$$d_L = \sqrt{\frac{\mathcal{L}}{4\pi\mathcal{F}}} = (1+z)r$$

Example:
SNIa

Angular distance d_A vs. redshift z

Proper diameter - d

Observed angular diameter – θ

$$\theta = d/(a r)$$

$$d_A \equiv \frac{d}{\theta} = a(t_1)r \rightarrow$$

$$d_L = (1+z)^2 d_A$$

Example:
Peaks in CMB spectrum

Need
“standard feature”

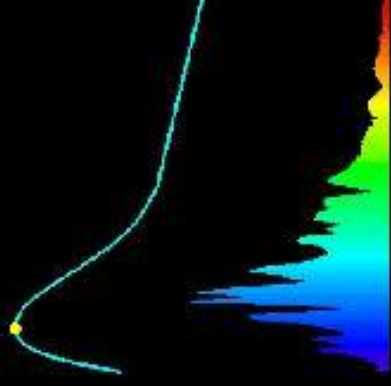
Evidence for Accelerated Expansion

Direct and Indirect

- **Cosmic Microwave Background** : inhomogeneities in radiation
- **Large Scale Structure** : inhomogeneities in matter object counts: galaxies, clusters, weak lensing, strong lensing, ...
- **SuperNovae Ia** – most direct

DÉFINITION La supernova de type Ia

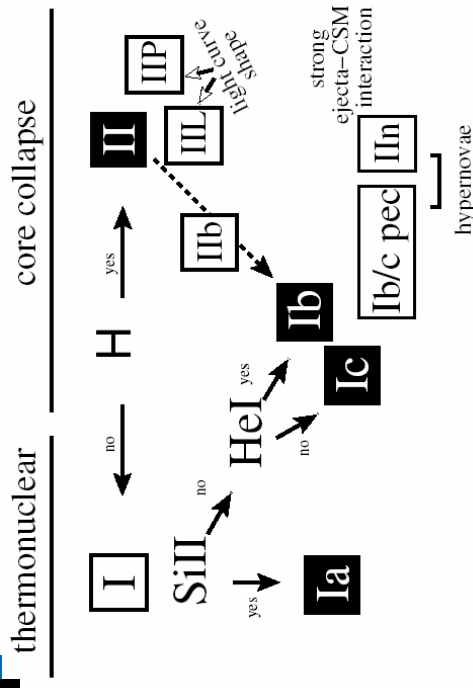
UNE ÉTOILE NAINE BLANCHE, RÉSIDU D'UN VIEUX SOLEIL, qui cohabite avec une étoile géante rouge, va progressivement chapper la matière de cette dernière. Quand la masse de la naine blanche atteint 1,4 fois celle du Soleil (masse de Chandrasekhar), des réactions thermonucléaires s'enchaînent, et la petite



מתאם בין בהירות שיא, צורה וספקטרום של עקומת האור ~ 10% פיזור בבהירות שיא

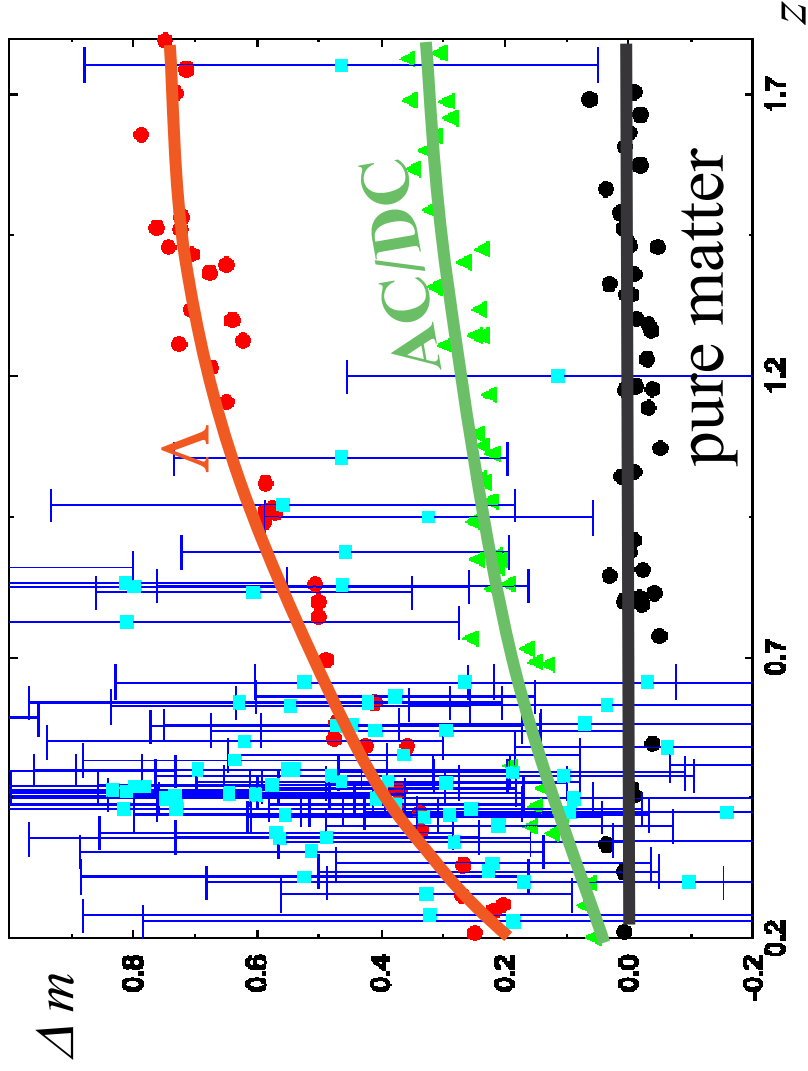


arXiv:astro-ph/0301107 v1 7 Jan 2003



Current SNIa Data

Cosmological Results from High-z Supernovae^{1,2}
 arXiv:astro-ph/0305008 v1 1 May 2003



Λ preferred

$$\Delta m = \frac{5}{\ln 10} \frac{\Delta d_L}{d_L}$$

$$\Delta m \approx \frac{\Delta L}{L}$$

fiducial models:

$$\Omega_m = 0.3$$

$$w_Q = \text{const.}$$

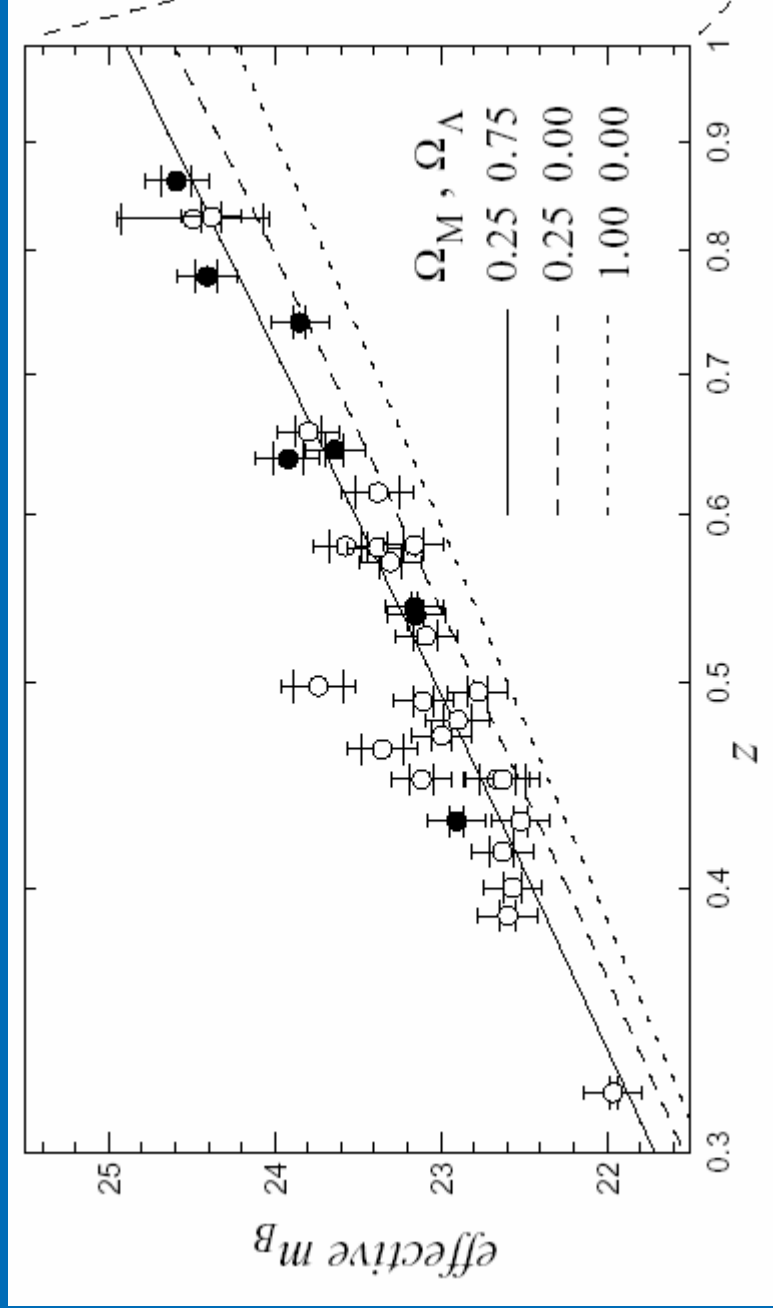
more distant \rightarrow

$$m(z) = M + 25 + 5 \log_{10} [H_0 d_L(z)]$$

Key issue: systematic errors

Previous version: Sci. Am. 1/2001

arXiv:astro-ph/0309368 v1 12 Sep 2003



Current Data



w_Q

- Ω_m vs. w_Q

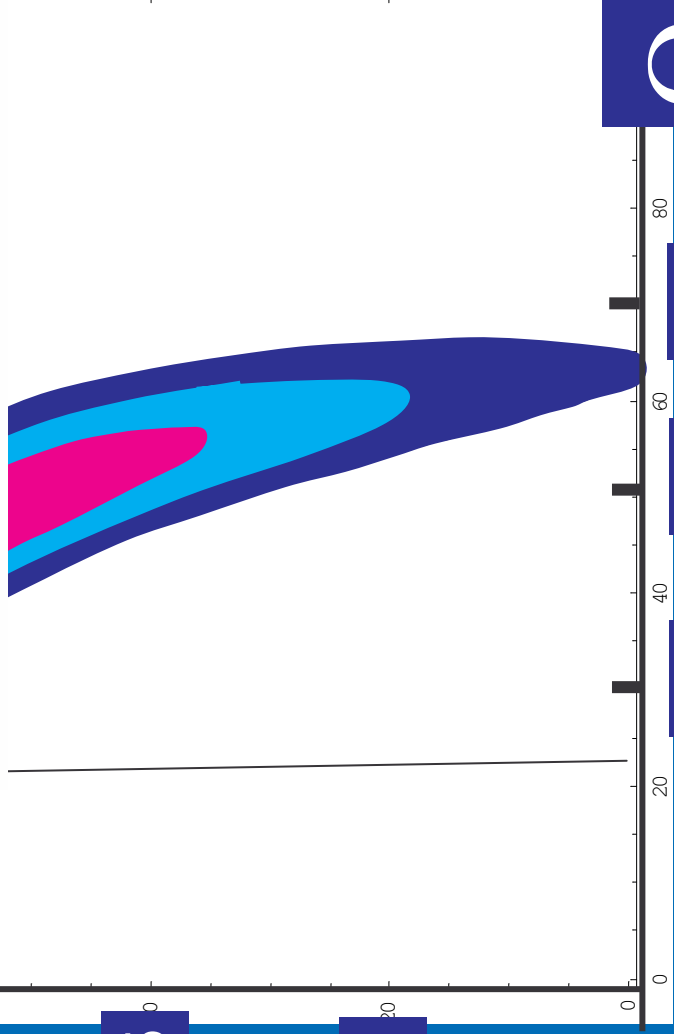
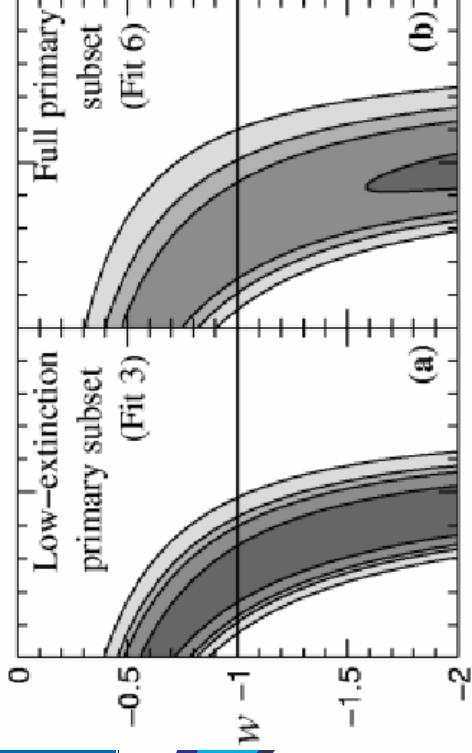
(assume flat U.)

$$w_T = \frac{p_T}{\rho_T} =$$

$$\frac{p_m + p_Q}{\rho_m + \rho_Q} = w_Q \Omega_Q =$$

$$w_Q (1 - \Omega_m)$$

Knop *et. al.* (2003)



0.3

0.5

0.7

Ω_m

$$DM \equiv 5 \log \left(\frac{D_L}{10 \text{ pc}} \right)$$

$$z \approx \frac{v}{c} = \frac{d}{D_H}$$

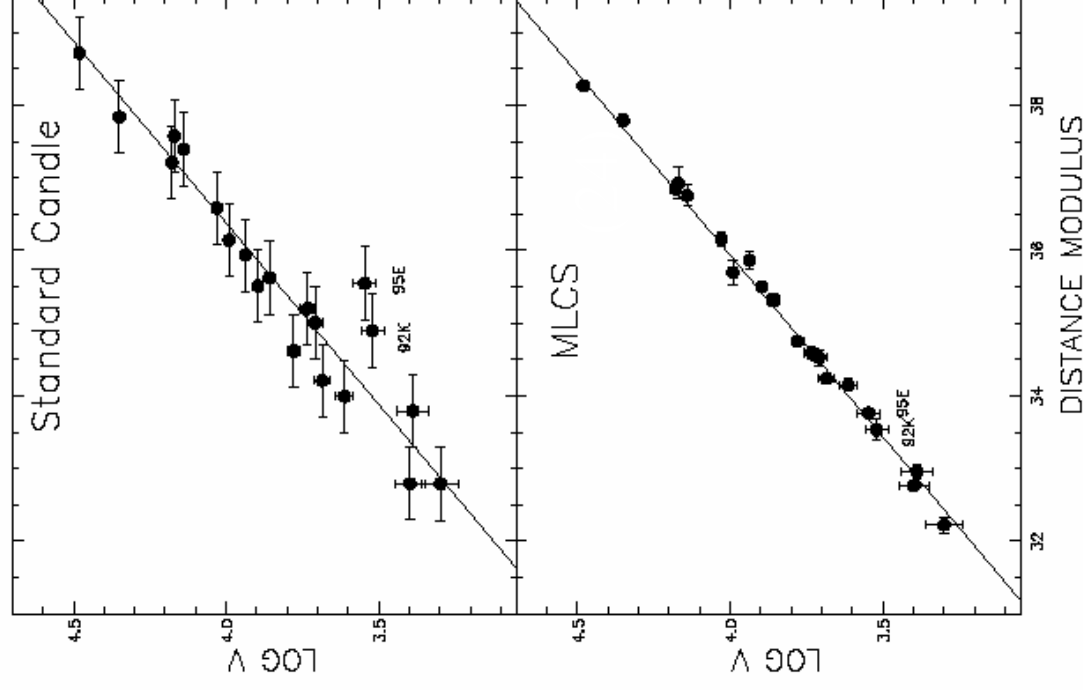
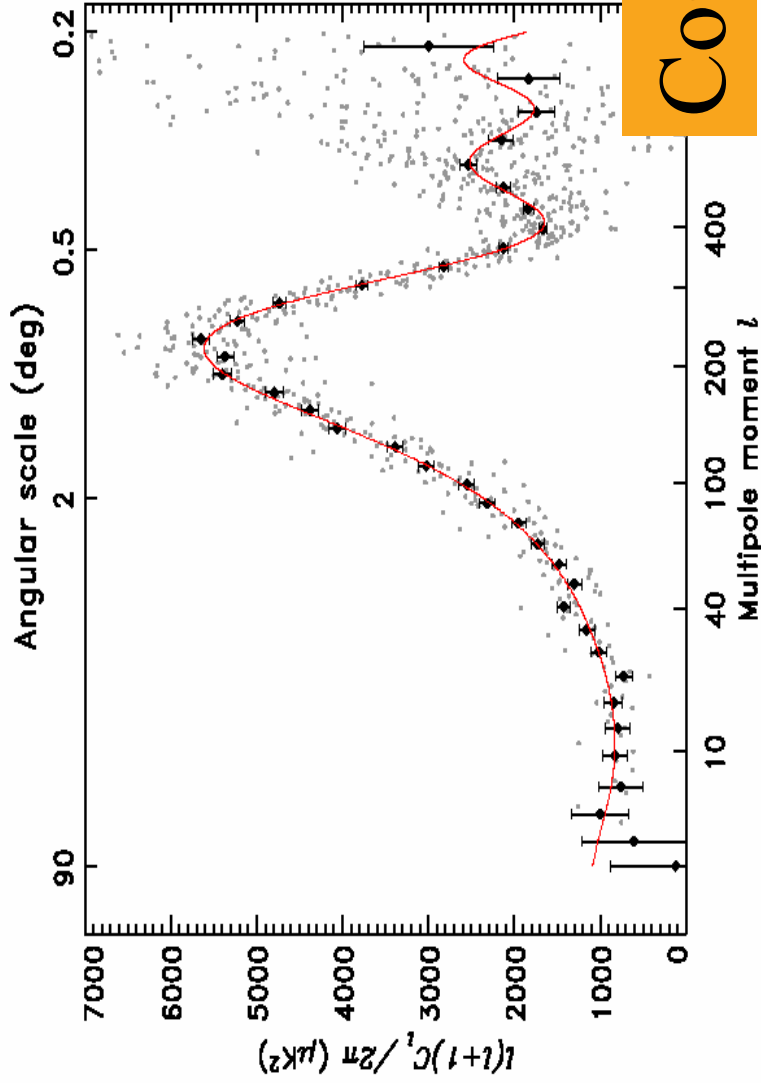
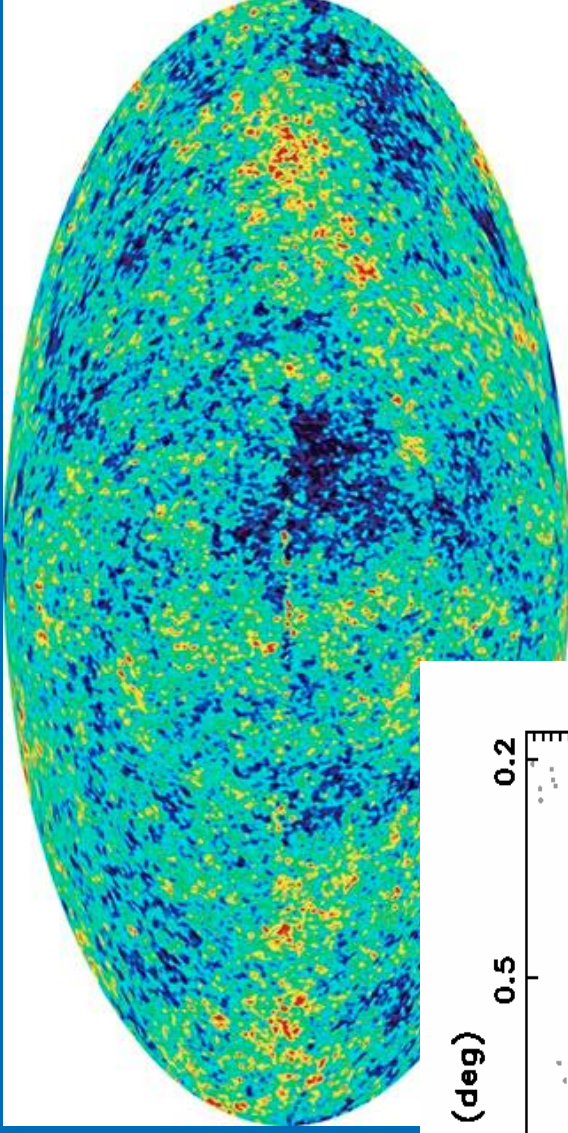


Figure 2. The Hubble diagram for SNe Ia before (top panel) and after (bottom panel) correction of the width–absolute brightness relationship. The figure is from Riess, Press & Kirshner (1995a).

CMB data : WMAP



$$\Theta(\hat{n}) = \Delta T/T.$$

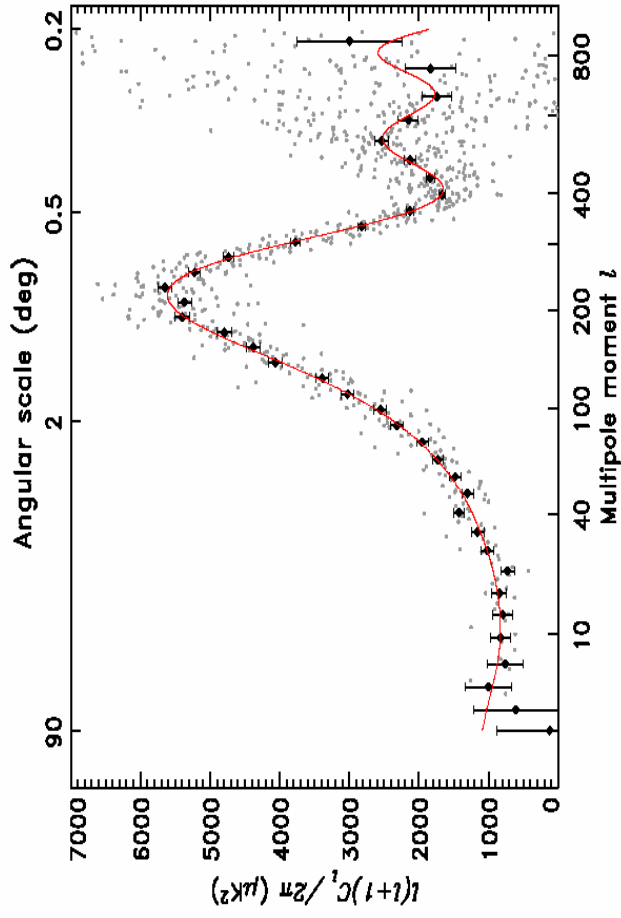
$$\langle \Theta_{\ell m}^* \Theta_{\ell' m'} \rangle = \delta_{\ell\ell'} \delta_{mm'} C_\ell$$

$$\Delta_T^2 \equiv \frac{\ell(\ell+1)}{2\pi} C_\ell T^2$$

Cosmic variance!

$$\Delta C_\ell = \sqrt{\frac{2}{2\ell+1}} C_\ell.$$

February 2003



One more point on the
Hubble diagram

($z \sim 1,000$)

$\ell_1 = 220 \cdot 1 \pm 0.8$

\sim Flat U.

Cosmic variance!

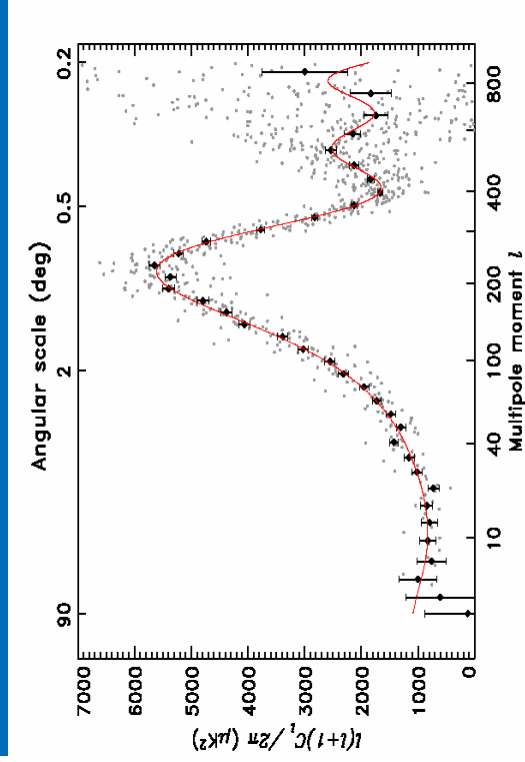
$$\Delta C_\ell = \sqrt{\frac{2}{2\ell + 1}} C_\ell.$$

Last scattering: U. becomes transparent

$$\frac{X_e^2}{1 - X_e} = \frac{Z_e Z_p}{Z_H} \sim 1.4 \times 10^{17} \frac{1}{\Omega_b^{0.05} h_{75}^2} \left(\frac{1 \text{ eV}}{T}\right)^{3/2} e^{-13.6 \text{ eV} / kT}$$

$$\Rightarrow kT_{90\%} \sim 0.3 \text{ eV}, kT_{ls} \sim 0.26 \text{ eV}$$

$$z_{ls} = T_{ls} / T_{today} = 26 \text{ eV} / 2.72 \text{ K} \sim 1100$$



A picture of the state of CMB photons @ $1s$
 = convoluted with their motion through the (whole) universe

Acoustic peaks

From: Hu & Dodelson (2002)

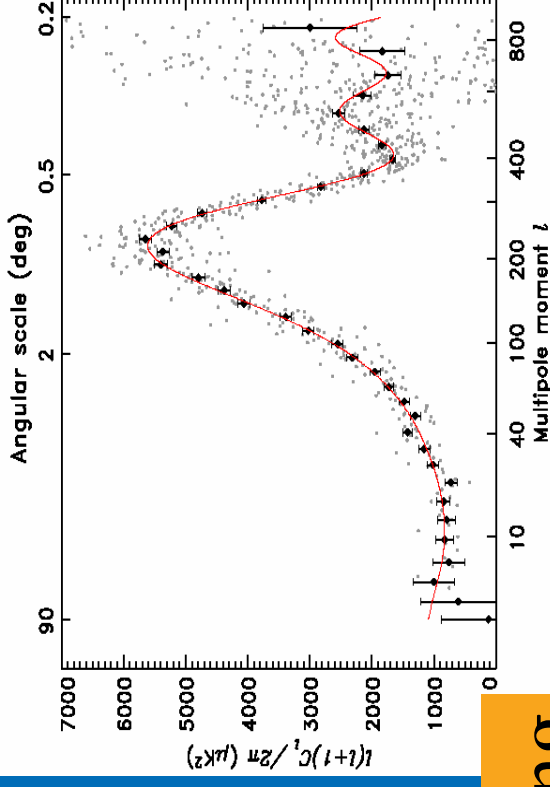
eq. without gravity

$$\ddot{\Theta} + c_s^2 k^2 \Theta = 0,$$

$$c_s \equiv \sqrt{\dot{p}/\dot{\rho}} = 1/\sqrt{3}$$

$\eta \equiv \int dt/a(t)$, for light $r = \eta$

fluid wave heating & cooling



solution $\Theta(\eta_{ls}) = \Theta(0)\cos(k s_{ls})$

no initial velocity

Sound horizon $s_{ls} = c_s \eta_{ls}$

$$\ell_n \approx n\pi D_{ls} / s_{ls, \text{max}}$$

Modes “caught” at
max./min.@ $ls \rightarrow$
peaks in PS

With gravity: $\Theta \rightarrow \Theta + \Psi$

Combined results

astro-ph/0302209 Table 7. Best Fit Parameters: Power Law Λ CDM

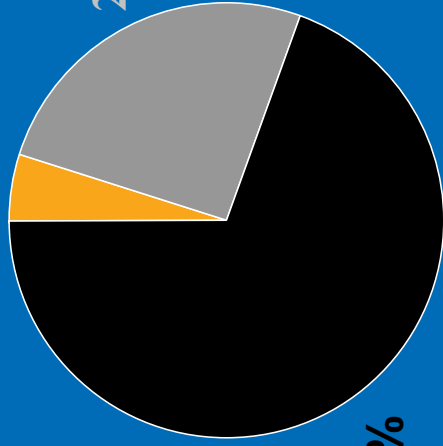
	WMAP	WMAPext ^{16a}	WMAPext+2dFGRS	WMAPext+ 2dFGRS+ Lyman α
A	0.9 ± 0.1	0.8 ± 0.1	0.8 ± 0.1	$0.75^{+0.08}_{-0.07}$
n_s	0.99 ± 0.04	0.97 ± 0.03	0.97 ± 0.03	0.96 ± 0.02
τ	$0.166^{+0.076}_{-0.071}$	$0.143^{+0.071}_{-0.062}$	$0.148^{+0.073}_{-0.071}$	$0.117^{+0.057}_{-0.053}$
h	0.72 ± 0.05	0.73 ± 0.05	0.73 ± 0.03	0.72 ± 0.03
$\Omega_m h^2$	0.14 ± 0.02	0.13 ± 0.01	0.134 ± 0.006	0.133 ± 0.006
$\Omega_b h^2$	0.024 ± 0.001	0.023 ± 0.001	0.023 ± 0.001	0.0226 ± 0.0008
χ^2_{eff}/ν	1431/1342	1440/1352	1468/1381	



Interim report I

- flat universe
- acceleration
- consistent
- reasonable ?!

4- 6%



■ Baryons
■ Dark matter
■ Dark energy

60- 80%

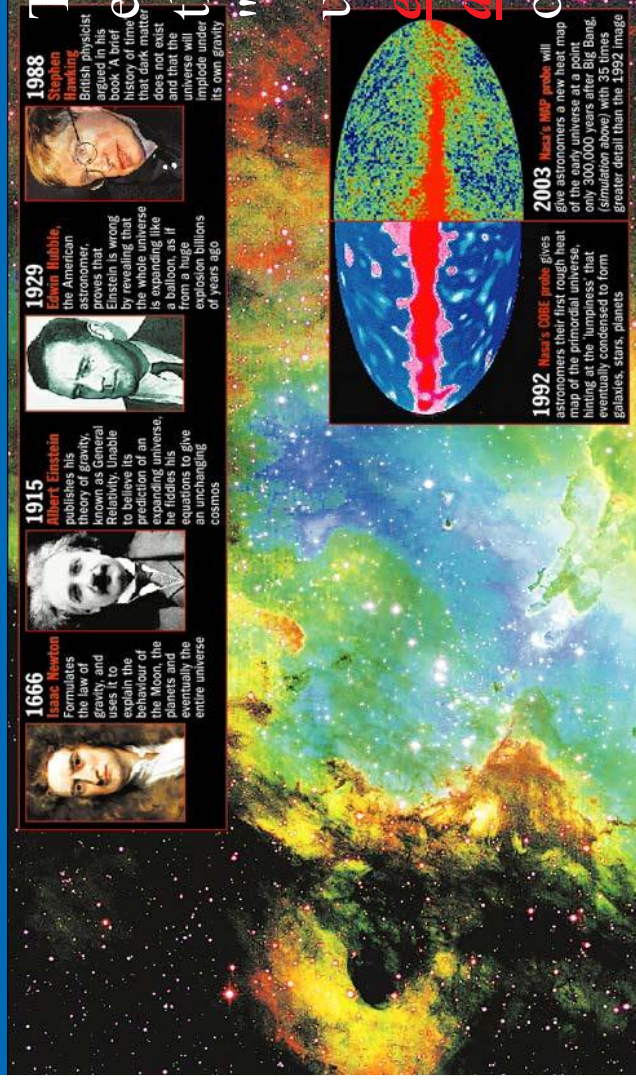
ν small

The end of the universe is cancelled

By Robert Matthews, Science Correspondent

(Filed: 09/02/2003)

Professor Hawking, we have a problem. Nasa, the American space agency, is expected to announce this week that it has proved the existence of "dark energy", a cosmic force that counteracts gravity and will keep the universe expanding forever.



The announcement will effectively demolish the theory that life will be wiped out in a "Big Crunch" when the universe collapses, and should end decades of academic dispute over the forces at work on the universe

Interpretation: theoretical expectations

- Dark energy is not just Λ
- Dynamical field (s):
 - Kinetic & potential energies
 - Interactions with other particles
 - Cosmic friction
 - Very small mass

→ time-dependence

Dark Energy EOS

- Parametrization in terms of (time-dependent)

Energy density $\rho_Q(z)$

Pressure $p_Q(z)$

EOS $w_Q(z) = p_Q(z) / \rho_Q(z)$

- previously: $w_Q = -1 \rightarrow \Lambda$

$w_Q = 0 \rightarrow$ cold matter

oscillations, “sudden start”, “decay to a constant”

Luminosity distance d_L vs. redshift z

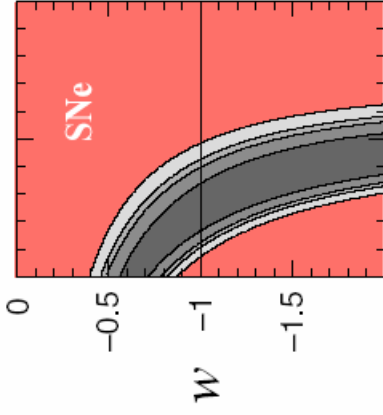
$$\begin{aligned} d_L &= \frac{(1+z)}{H_0} \int_1^{1+z} dx \exp \left[-\frac{3}{2} \int_1^x (1+w_T(y)) \frac{dy}{y} \right] = \\ &= \frac{(1+z)}{H_0} \int_1^{1+z} dx \frac{dx}{x^{3/2}} \exp \left[-\frac{3}{2} \int_1^x \left(\frac{w_Q(y)}{1+g} \exp \left[-3 \int_1^y w_Q(u) \frac{du}{u} \right] \right) \frac{dy}{y} \right] \end{aligned}$$

$$g = \Omega_m / (1 - \Omega_m)$$

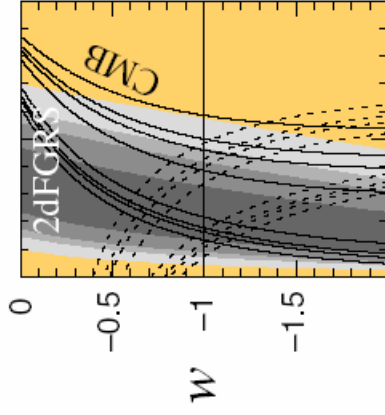
Maor et al.

Current SnIA data: some acceleration in the last 8 billion years ($0 < z < 1$)

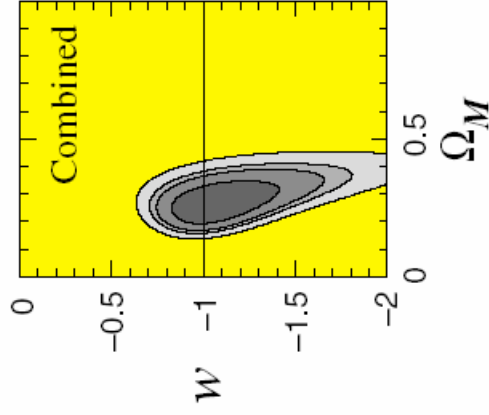
Supernova Cosmology Project
Knop et al. (2003)



Assuming constant w



With limits from;
2dFGRS (Hawkins et al. 2002)
and CMB (Bennet et al. 2003,
Spergel et al. 2003)



$$w = -1.05^{+0.15}_{-0.20} \text{ (statistical)}$$
$$\pm 0.09 \text{ (systematic)}$$

Current SNIa Data

Fit to

$$w_Q = w_0 + w_1 z$$

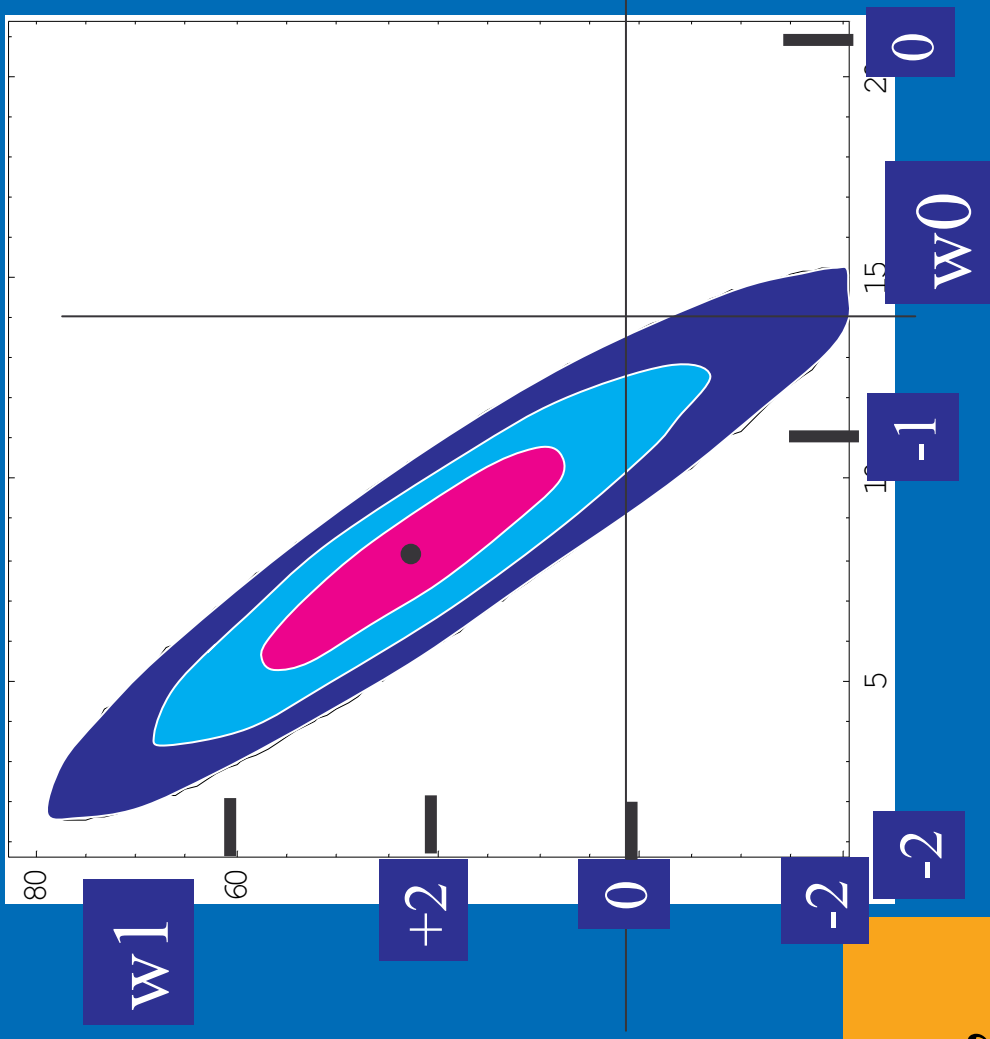
* Fixed $\Omega_m = 0.23$

(Fixed $\Omega_m = 0.32$,

$$0 < w_1 < +4, 1\sigma)$$

$w_Q < -.7$ for some z ,

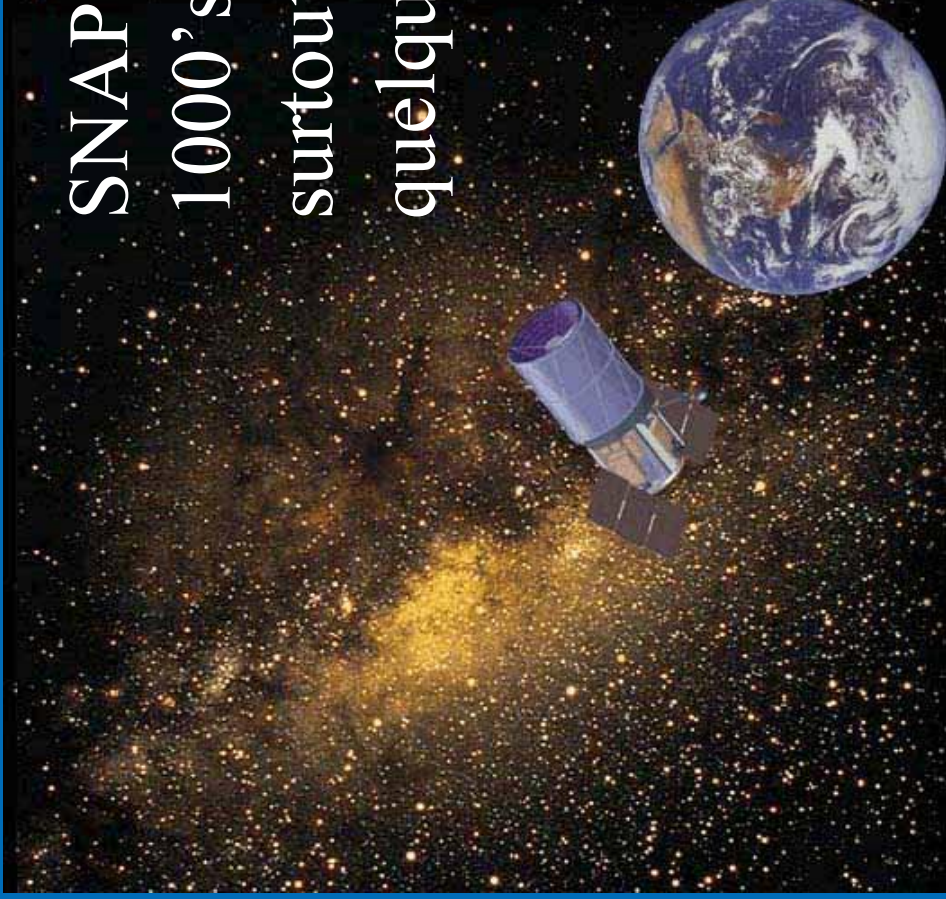
$$0 < z < 1$$



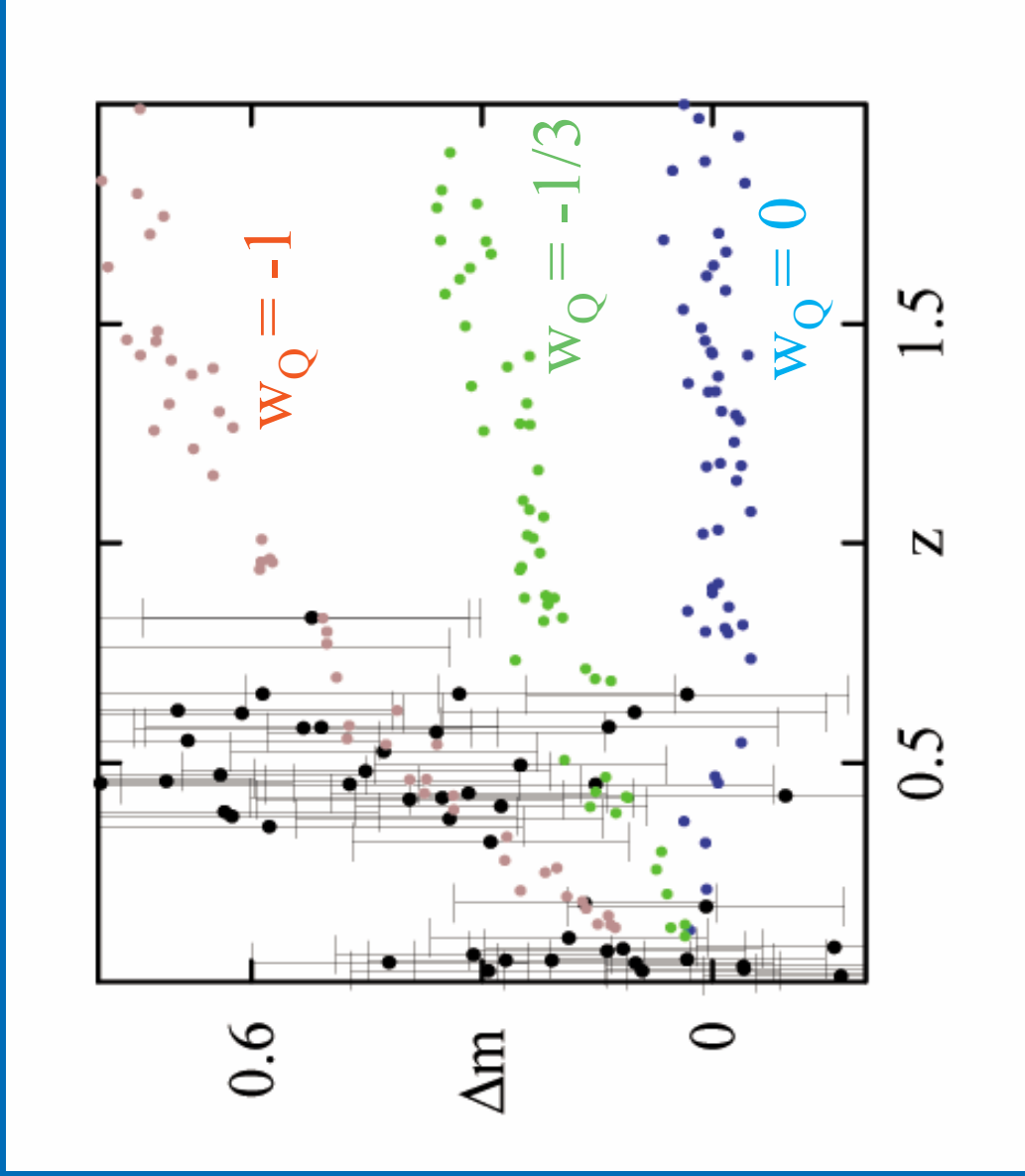
L'avenir: SNAP (F)

snap.lbl.gov

SNAP proposal:
1000's de SNIa,
surtout $0 < z < 1.2$,
quelques-uns $1.2 < z < 1.7$



Also:
ESSENCE
CFHLS (F)
GOODS,
SNFactory (F)



fiducial
models:
 $\Omega_m = 0.3$
 $w_Q = \text{const.}$

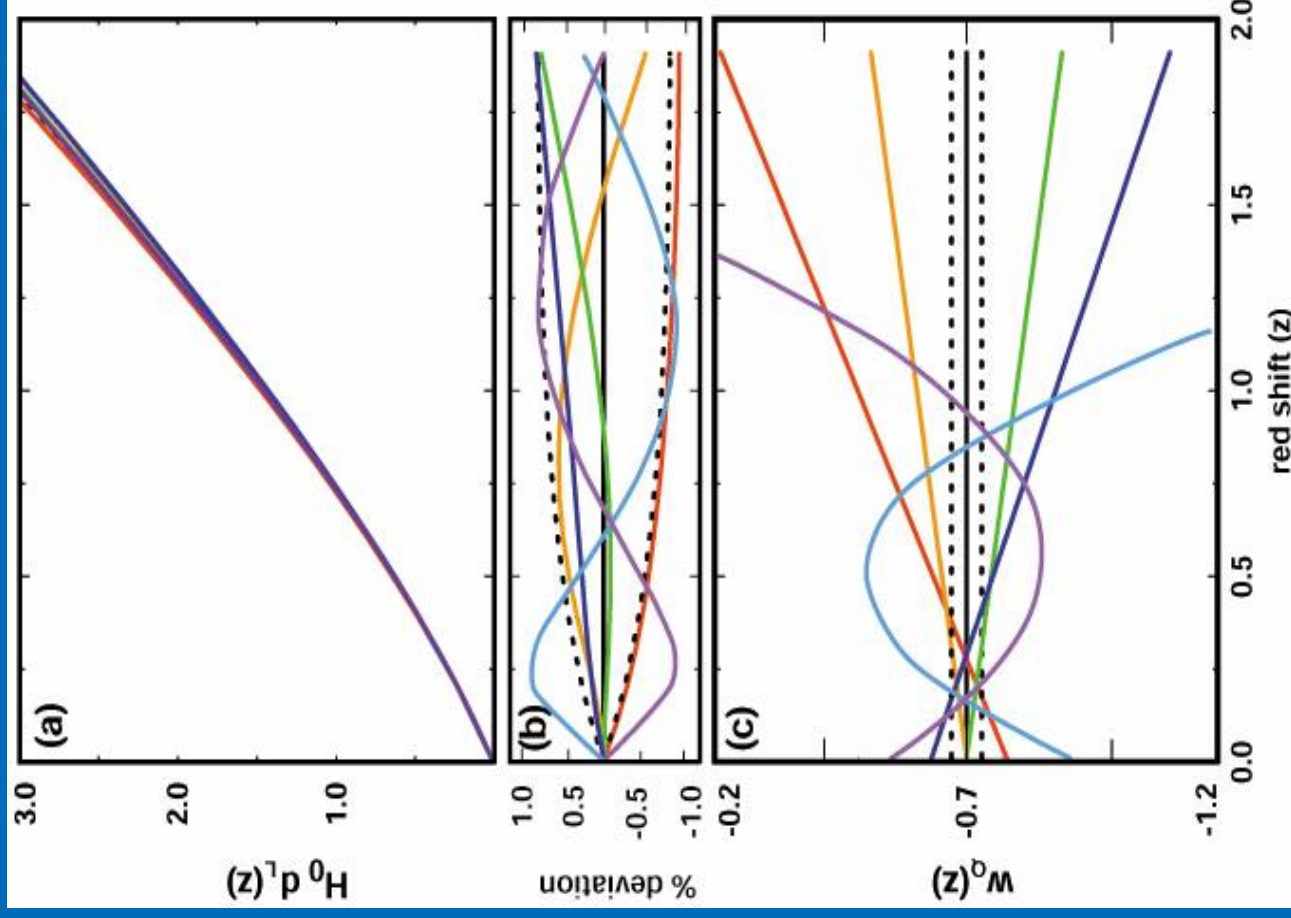
See: Sci. Am. 1/2001

Degeneracy!

Maor et al.

- a) DL
- b) Δ DL/DL
- c) $w_Q(z)$

For 9 different EOS



CMB cannot help much ...

Maor & Brustein

- Dark energy expected to “disappear” for $z > 2$
- CMB photons propagate most of the way through matter dominated U.
 - No gain compared to “low z ” probes
- Best accuracy for d_L from CMB $\sim 1\%$
 - CMB comparable to other probes

- CMB cannot help much ...

Maor & Brustein

$$\begin{aligned}
 d_L(x_{ls}) &= x_{ls} \int_1^{x_{ls}} \frac{dx}{H(x)} \\
 &= x_{ls} \int_1^3 \frac{dx}{H(x)} + x_{ls} \int_3^{x_{ls}} \frac{dx}{H(x)} \\
 &= \frac{x_{ls}}{3} d_L(3) + \frac{x_{ls}}{H(3)} \int_3^{x_{ls}} \frac{dx}{H(x)/H(3)} \\
 &= \frac{x_{ls}}{3} d_L(3) + \frac{x_{ls}}{H(3)} \int_3^{x_{ls}} \frac{dx}{(x/3)^{3/2}} \\
 &= \frac{x_{ls}}{3} d_L(3) + 2x_{ls} \left(\frac{1}{\sqrt{3}} - \frac{1}{\sqrt{x_{ls}}} \right) \left(\frac{3^{3/2}}{H(3)} \right),
 \end{aligned}$$

$$d'_L(3) = c_1 \frac{d_L(3)}{3}$$

$$\Delta d'_L(3) = c_2 \frac{\Delta d_L(3)}{3}$$

$$\left(\frac{\Delta d_L}{d_L} \right)_{x_{ls}} \simeq \frac{2c_2 - 1}{2c_1 - 1} \left(\frac{\Delta d_L}{d_L} \right)_{x=3}$$

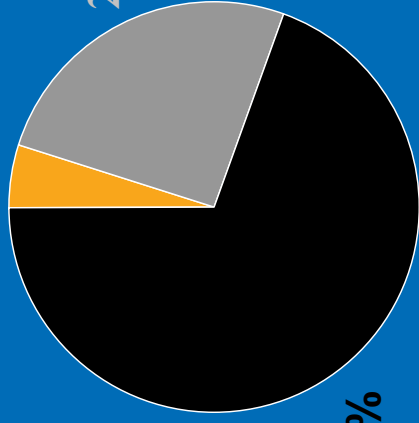
$$x=z+1$$

Interim report II

- recent acceleration
($0 < z < 1$, today $< t < 8$ billion years)
- evidence from many sources, consistent.
- qualitative information only (on
fundamental physics) from most accurate
planned experiments

Dark sector & the standard model of particle physics

4- 6%
20- 40%



■ Baryons

■ Dark matter

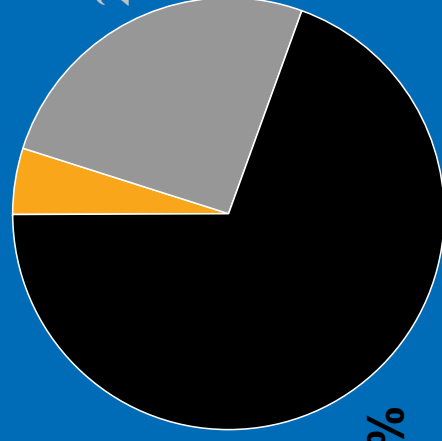
■ Dark energy

arXiv:hep-ph/0211065 v1 5 Nov 2002

$$\begin{aligned} M_H &= 86^{+49}_{-32} \text{ GeV}, \\ m_t &= 174.2 \pm 4.4 \text{ GeV}, \\ \alpha_s &= 0.1210 \pm 0.0018, \\ \hat{\alpha}(M_Z)^{-1} &= 127.922 \pm 0.020 \\ s_Z^2 &= 0.23110 \pm 0.00015, \\ \bar{s}_\ell^2 &= 0.23139 \pm 0.00015, \\ s_W^2 &= 0.22277 \pm 0.00035 \\ s_{M_Z}^2 &= 0.23105 \pm 0.00008 \end{aligned}$$

Dark sector & gravity and quantum mechanics

4-6%
20-40%



■ Baryons

■ Dark matter

■ Dark energy

$$\rho_{Vacuum} = \sum_{\omega} \frac{1}{2} \hbar \omega$$

$$G_{00} = 8\pi G_N \rho$$

Does not make sense
as a normal source

P. J. E. Peebles :

arXiv:astro-ph/0209403 v1 19 Sep 2002

Abstract. Physical science has changed in the century since Lord Kelvin's celebrated essay on *Nineteenth Century Clouds over the Dynamical Theory of Heat and Light*, but some things are the same.

Cloud No. I: the Dark Sector

Cloud No. II: Strong Spacetime Curvature



Cloud No. III: the Me



"We live where we can live,"

NYT: 2 Sept. 2003

Something has to give

- Gravity
- $\rho_{Vacuum} = \sum_{\omega} \frac{1}{2} \hbar \omega$
 $G_{00} = 8\pi G_N \rho$
- Matter – additional fields, light, extremely weakly coupled – “quintessence”
- Quantum mechanics
- More space dimensions
- Cherished principles: causality, ...

**and the ugliest(?) of them all:
the Anthropic principle**

The “boring” option: Quintessence

Maor & Brustein

Degeneracies

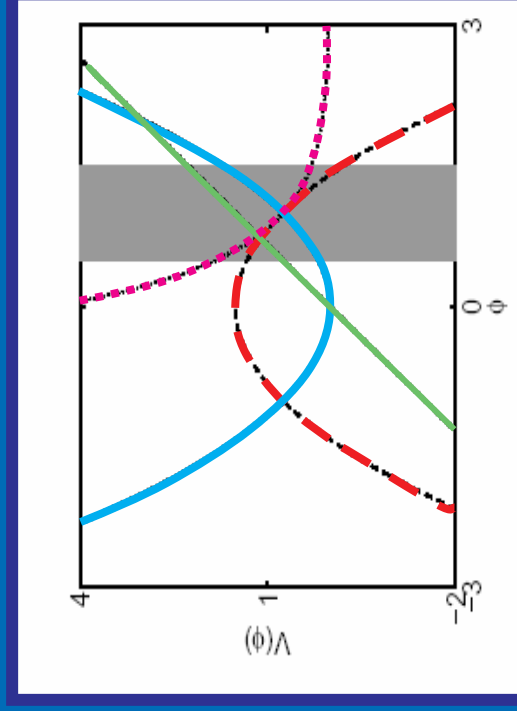
$$\begin{aligned}w_Q &= \frac{p_Q}{\rho_Q} \\ &= \frac{x^2 H^2 \phi'^2 - 2V}{x^2 H^2 \phi'^2 + 2V}.\end{aligned}$$

- “Tracker” fields
- Many other possibilities

$$m \sim H = 10^{-33} \text{ eV}$$

$$V \sim \rho_{crit} \sim (10^{-3} \text{ eV})^4$$

Steinhardt + ...
Ratra+Peebles
Wetterich ...



The Anthropic Principle

R. Dicke (1961): “ carbon-based life can only arise when the Dirac large numbers hypothesis is true because this is when burning stars exist”

B. Carter (Early 1970's): “what we can expect to observe must be restricted by the conditions necessary for our presence as observers” (Leslie ed. 1990). The word "anthropic" was intended as applying to intelligent beings.

A possible argument for preferring the God hypothesis: think in terms of many possible fundamental theories, God selecting a theory which permitted life's requirements to be fulfilled without contradictions.

Conclusions

- **Excellent measurements are not good enough as clues for fundamental physics !**
- **A large source of error: theory**
- **Need:**
 - **either a new “local” test -what is it?**
 - **or radically new theoretical input -what is it ?**
- **Theory situation in a nut-shell**
“we don’t have a clue”
- **Personal hope: revolutionary resolution**